Effects of severe hallux valgus on metatarsal stress and the metatarsophalangeal loading during balanced standing: A finite element analysis

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Abstract

The internal stress of the human foot enables efficient parametric evaluation of structural and functional impairments associated with foot deformities, such as hallux valgus (HV). However, the status of the internal stress of such a deformed foot remains insufficiently addressed due to the difficulties and limitations of experimental approaches. This study, using finite element (FE) methodology, investigated the influence of severe HV deformity on the metatarsal stress and the metatarsophalangeal (MTP) joint loading during balanced standing. FE models of a normal foot and a severe HV were constructed and validated. Each FE model involves 28 bones and various cartilaginous structures, ligaments, and plantar fascia, as well as encapsulated soft tissue. All the materials except for the encapsulated soft tissue were considered isotropic and linearly elastic, while the encapsulated soft tissue was set as nonlinear hyperelastic. Hexahedral elements were assigned to the solid parts of bones, cartilage, and the encapsulated soft tissue. Link elements were assigned to ligaments and plantar fascia. A plate was created for simulating ground support. A vertical force of a half-body weight was applied on the bottom of the plate for simulating balanced standing loading. The superior surfaces of the encapsulated soft tissue, distal tibia, and distal fibula were fixed. Stress distribution in the metatarsals, contact pressure, and force at the MTP joints were comparatively analysed. Compared to the normal foot, the HV foot showed higher stress concentration in the metatarsals but lower magnitude of MTP joint loading. In addition, the region with high contact pressure at the first MTP joint shifted medially in the HV foot. Knowledge of this study indicates that patients with severe HV deformity are at higher risk of metatarsal injuries and functional impairment of the MTP joints while weight bearing.

Keywords: Finite element, Severe hallux valgus, Metatarsal stress, Metatarsophalangeal loading

1. Introduction
Hallux valgus (HV) is a common foot deformity characterized by progressive lateral deviation of the hallux with medial deviation of the first metatarsal. Indexes of hallux valgus angle (HVA) and intermetatarsal angle (IMA) are commonly used radiological measurements for assessing the degree of deformity, which is classified as mild (HVA: 15°–20°; IMA: 9°–11°), moderate (HVA: 20°–40°; IMA: 11°–16°), and severe (HVA: >40°; IMA: >16°) [1]. Increasing HV severity may cause significant health-related problems, such as metatarsalgia [2], balance deficits [3], and increase in risk of falling in older people [4].

Because the metatarsal bones act as a unit in the forefoot area to provide a broad plantar surface for load bearing, the majority of research on biomechanical consequences of HV deformity have referred to the alternation of forefoot loading recorded by plantar pressure measurements. HV deformity has been reported as resulting in increased forefoot plantar pressure, with debate about which region the change occurs in. Some studies have suggested that the peak pressure increased significantly under the first and second metatarsals in HV feet compared with that in normal feet [5,6,7,8]. There is contrary evidence that HV deformity causes increased load on the lateral metatarsals [2,9]. Koller et al. [10] assessed the plantar pressure of HV feet of different grades and found a positive correlation between HV grade and the peak pressure of the fifth metatarsal head. On the other hand, changes in the loading state of the inner foot are poorly explored.

As a result of the intrinsic difficulties and limitations of conventional experimental methods, the internal loading of cartilaginous and bony structures cannot be measured directly. Finite element (FE) methodology is increasingly used to simulate the mechanical responses of biological systems via a numerical model simulating complicated boundary and loading conditions. The FE model is capable of predicting the internal stress in the foot complex and eventually interpreting potential risks associated with foot deformities. Through reducing the stiffness of ligaments, Wong et al. [11] developed a FE foot model of first ray hypermobility which presented higher resultant metatarsocuneiform joint force along with an abrupt change in medial-lateral direction. They interpreted failure of the joint to accommodate the change of joint...
as possible deviation of the first metatarsal from normal alignment, possibly causing metatarsus primus varus. Extrinsic factors, such as high-heeled shoes, have been reported to be responsible for the occurrence of foot disorder. Using FE method, Yu et al. [12] suggested that the increased von Mises stress over the lateral and dorsal regions of the first metatarsophalangeal (MTP) joint during prolonged high-heeled standing may induce the development of HV deformity. Wong et al. [13] assumed HV deformity to be a normal foot with hypermobility and manifested that the arthrodesis of the first metatarsocuneiform is a useful treatment for functional restoration of HV based on the increased compressive stress in the first metatarsal. Furthermore, a subject-specific FE model of HV foot was developed recently to compare the effects of different surgical fixation methods on HV treatment by predicting the peak von Mises stress and compression stress of the distal fragment of the first metatarsal [14]. Information on stress distribution of the internal structures is useful in enhancing the understanding of podiatric biomechanics and may contribute to surgical treatments. In this study, FE foot models of a normal subject and a severe hallux valgus (HV) patient were developed to evaluate the metatarsal stress and the MTP joint contact pressure under a balanced standing condition. It was hypothesized that metatarsal stress would increase while the MTP joint contact pressure would decrease in the severe HV foot.

2. Material and methods

2.1 Model construction

This study has been approved by the Human Ethics Committee of Ningbo University (ARGH20170213). HVA and IMA for the HV foot were 48.07° and 16.17°, respectively; and those for the normal foot were 22.82° and 14.14°, respectively (Figure 1). The three-dimensional models of the normal foot and the HV foot were reconstructed from computer tomography (CT) images of a 26-year old female (height: 165cm; weight: 51kg) and a 37-year
old female (height: 163cm; weight: 52kg) respectively. Both participants had no other musculoskeletal pathology, pain, or lower limb injury or surgery within the past 12 months. The coronal CT images were obtained with a space interval of 2 mm without weight-bearing from the left foot. The two-dimensional images were segmented using MIMICS 16.0 (Materialise, Leuven, Belgium) to obtain the three-dimensional model of the bone tissue and the encapsulated soft tissue. The uneven surface of the geometries of the bony components and the soft tissue were smoothed using Geomagic Studio 2013 (Geomagic, Inc., Research Triangle Park, North Carolina, USA). Each surface component was then imported into Solidworks 2016 (SolidWorks Corporation, Massachusetts, USA) individually to form a solid part. To model a cartilaginous structure, a solid volume was created between the adjacent surfaces of two bones, and the bones were then subtracted from the solid volume. All bones and cartilage were subtracted from the full volume of soft tissue to create the encapsulated soft tissue. The numerical foot model consisted of 28 bony segments, including tibia, fibula, talus, calcaneus, cuboid, navicular, three cuneiforms, five metatarsals, and 14 phalanges. Link elements that have tension-only capability were used to model ligaments. A total number of 76 ligaments and five plantar fascia were included and defined by connecting attaching points on corresponding bones with straight line structures. The attaching regions were determined by reference to an anatomy book [15] and the attaching points were approximately close to the geometrical centre of the attaching regions. The plantar fascia consisted of five separate rays connecting the insertions between the calcaneus and the proximal phalanges. The plantar ligaments and the spring ligament were represented by two separate rays, and small ligaments were represented by a single ray. HyperMesh 13.0 (Altair Engineering Inc., Hyperworks, America) was used for mesh generation. Each bony and cartilaginous component and the encapsulated soft tissue were partitioned into sub-volumes and then assigned hexahedral elements for each volume. The mesh size for both models was 4.5 mm for the encapsulated soft tissue, 3 mm for the bones, and 2.5 mm for the cartilaginous structures. Mesh sensitivity tests were conducted on the whole foot model under conditions of balanced standing by gradually reducing the mesh sizes. An
acceptable mesh generation is determined as the deviation of resultant peak equivalent stress (PES) in
the first metatarsal, and the calcaneus was within 5% when further reducing mesh sizes. For the normal
foot model, the deviation of PES in the first metatarsal and the calcaneus were 1.56% and 2.24%, respectively;
and for the HV foot model, the deviation data were 2.38% and 3.82%, respectively. The total number of
elements for the normal foot model was 195,237 and that for the HV foot model was 180,885. The FE
package ANSYS Workbench 17.0 (ANSYS, Inc., Canonsburg, USA) was used for subsequent analysis. This software
provides automated contact detection for assemblies. Using algorithms based on surface proximity, it is able to
create possible contact pairs. Surface-to-surface contact was used to simulate the interaction of the
surfaces of the cartilaginous and bony structures. The contact between bone and cartilaginous surfaces was
assumed as frictionless [16, 17]. All the bones and cartilage were bonded to the encapsulated soft tissue.
All the materials except for the encapsulated soft tissue were considered isotropic and linearly elastic with
properties obtained from previous literature [17, 18]. The two material constants of Young’s modulus $E$ and
Poisson’s ratio $\nu$ were assigned to represent the elasticity. The encapsulated soft tissue was set as nonlinear
hyperelastic material which was defined as a Moonley-Rivlin model. The element types and material
properties used are listed in Table 1 and Table 2.

2.2 Load and boundary conditions

A balanced standing condition was considered for the FE analysis. The superior surfaces of the
encapsulated soft tissue, distal tibia, and distal fibula were fixed (Figure 2). A plate was created
assigned with an elastic property to model the ground support (Table 1). The plate was allowed
to move freely only in the vertical direction. A vertical ground reaction force (GRF) of a half-body
weight (255 N for normal foot; 260 N for HV foot) was applied at the inferior surface of the plate. The interaction between the foot and the plate was simulated as contact surface with a coefficient of friction of 0.6 [12]. Five equivalent force vectors representing the Achilles tendon
force were applied on the posterior extreme of the calcaneus. The force of the Achilles tendon (128 N for normal foot; 130 N for HV foot) was estimated as 50% of the load applied on the foot while balanced standing [25].

2.3 Model validation

The numerical model was validated by comparing plantar pressure obtained from computational simulation in FE software and experimental measurement by a Novel emed pressure platform (Novel, Munich, Germany) in a standing position. The measurement was performed on the same subject who had volunteered for the medical image scanning. Both subjects were asked to stand still on the pressure platform for five seconds. Data from the middle three seconds were selected and averaged. The validated models were then used for FE analysis on forefoot biomechanics.

3. Result

3.1. Model validation

Figure 3 shows the comparison of predicted plantar pressure (b, d) with experimental results (a, c). Pressure distribution from the FE result was generally consistent with the experimental result. Also, a good match between peak pressure value and location were found for both models (Figure 3). For the normal foot model, the peak pressure from prediction and measurement was 0.141 MPa and 0.135 MPa, respectively, and for the HV foot the values were 0.144 MPa and 0.137 MPa, respectively. The second highest pressure was located under the first metatarsal head for both models. The predicted pressure of the normal foot model and HV foot model was 0.089 MPa and 0.122 MPa, respectively, and the corresponding measured pressure was 0.093 MPa and 0.127 MPa, respectively. This suggests that the models are valid for further simulation.

3.2. Metatarsal von Mises stress
The von Mises stress in metatarsals generally increased due to HV deformity, as shown in Figure 4. For both the normal and HV foot, the third metatarsal experienced the highest von Mises stress concentration, followed by the second, fourth, and first metatarsals, and the lowest stress level existed at the fifth metatarsal. Compared to the normal foot, medial and lateral forefoot sustained a larger percentage of von Mises stress in the HV foot. The severe HV foot showed pronounced increases in von Mises stress at the fifth (55%), first (44%), and fourth (40%) metatarsals. For the third metatarsal, it was 4.12 MPa in the normal foot and increased to 4.24 MPa due to HV deformity. However, the stress concentration at the second metatarsal decreased (less than 3%) in the severe HV foot.

3.3. MTP joint contact pressure

The severe HV foot showed lower MTP joint contact pressure, especially at the second to fifth MTP joints (Figure 5). Contact pressure at the first MTP of the severe HV foot (0.28 MPa) was slightly lower than that of the normal foot (0.3 MPa). Figure 6 illustrates the apparently different locations of high contact pressure (Unit: MPa) at the first MTP joint between the severe HV foot and the normal foot. For the normal foot, the maximum pressure is located at central bottom of the contact surface, while for the severe HV foot it transfers medially so that it is located at medial bottom of the contact surface.

3.4. MTP joint force

The MTP joint force was defined as the reaction force imposed by the first metatarsal on the proximal/posterior surface of the cartilage between the first metatarsal and the proximal phalanx. The component MTP force was dominant in the anterior-posterior direction (4.58 N for the severe HV foot and 8.67 N for the normal foot), while it only accounted for 7.1% in the severe HV foot and 10% in the normal foot in medial-lateral and superior-inferior directions. The resultant MTP force of the severe HV foot was nearly 50% less than that of the normal foot (Figure 7).
4. Discussion

The development of a comprehensive computational model of the human foot was suggested for research focusing on podiatric biomechanics, so as to overcome the intrinsic limitations of in vivo experiments for further understanding of foot problems [26]. This study explored the effects of severe hallux valgus on metatarsal stress and on metatarsophalangeal joint loading while balanced standing using the FE method. The development of patient-specific models is advocated for foot problems with distinct structural deformity [27, 28]. Knowledge of this study would provide information for medical treatment of HV and subject-specific footwear design.

4.1. FE model of severe HV foot

Three-dimensional FE models were validated by plantar pressure measurement. This method was commonly used in the validation of a FE foot model [18]. In general, the predicted plantar pressure distribution and peak pressure were comparable to the experimental measurements. The material properties of the bony, cartilaginous, ligamentous, and encapsulated-soft-tissue components were considered consistent between the normal foot and the deformed foot. Many studies have developed normal-foot FE models or a pathological model from the normal one to investigate internal foot biomechanical performance under various conditions [28]. In an attempt to promote the understanding of HV pathomechanics and to improve the effectiveness of treatments, a FE model of the first ray has been constructed for predicting mechanical consequences of mild HV deformity [29]. An entire foot model featured with skeletal deformity of severe HV was also developed and validated in this study to provide potentials for research purposes and clinical application. Previous FE models relied heavily on the tetrahedral elements for meshing bones, cartilage, and soft tissue on account of the effort attributed to developing a hexahedral mesh of irregular geometry. In theory, the hexahedral element, due to its nature of having relatively more degrees of freedom, is able to provide more accurate FE analysis [30, 31]. Although one study modelling the proximal femur showed that tetrahedral and hexahedral
elements presented nearly the same resultant peak von Mises stress, the CUP time was significantly less when using hexahedral elements, indicating a more efficient computational foundation of the hexahedral element mesh scheme. The bony and cartilaginous components and the encapsulated soft tissue were meshed as hexahedral elements in this study, which was proposed to be utilized for better comparison of FE predicted results by Yu et al. [12]. To improve the mesh quality and the percentage of hexahedral elements, the individual bony and cartilaginous components and the soft tissue were partitioned prior to mesh generation in HyperMesh 13.0.

4.2. Metatarsal von Mises stress

The five metatarsal bones have an important function with respect to weight bearing. Previous experimental results advocated medial or lateral shift of forefoot plantar pressure due to HV deformity. This study predicted obviously higher plantar pressure under the first metatarsal head in the HV foot model than in the normal foot model, which is consistent with the outcomes measured by Martínez-Nova et al. [8]. As to the inner stress, the von Mises stress is often considered as one predictor for stress failure of foot bone which has been widely used for evaluating the risk of long-term pathological changes. Cheung et al. [32] noted that the intensified stress at central metatarsals and dorsal calcaneocuboid joint junction may lead to midfoot pain. This study found higher peak von Mises stress in the metatarsals, except for the second one for the severe HV foot, indicating an increasing risk of stress or fatigue failure. As balanced standing is the most common and basic behaviour in daily life, it can be speculated that the increased metatarsal stress may cause metatarsalgia while sustaining weight bearing. The most obvious increasing of von Mises stress at the fifth metatarsal indicates that the fifth metatarsal is more susceptible to injury for patients with severe HV. The first metatarsal should be expected to avoid high stress during weight bearing in cases of first ray deformity, however, the predicted stress at the first metatarsal for the severe HV foot was 44% higher than that of the normal foot. This is very likely to be associated with medial arch collapse, which is often thought to supervene with hallux valgus [33]. The crossover second toe also commonly occurs
in the presence of hallux valgus as shown in Figure 1 (a) [34]. The abnormal alignment of
second ray seems a possible factor leading to the slightly decreased stress of the second
metatarsal. It is important to note that the crossover second toe is not a definite condition
accompanied by hallux valgus, indicating that the crossing toes may hinder the generalization of
the findings.

4.3. MTP joint loading
The contact pressure of MTP joints was lower in the severe HV foot, especially for the second
to fifth MTPs. Similarly, the resultant joint force of the first MTP also showed lower magnitude
than that of the normal foot. The decreased joint loading may imply the impairment of load
bearing and transfer function of the first MTP joint in gait. In agreement with this speculation,
Zhang et al. [29] found weakened windlass mechanism in the HV foot during initial push-off.
As to the contact pressure of the first MTP joint, there is only a slight decrease for the severe
HV foot, while regions with high pressure locate apparently differently between the HV foot
and the normal foot. In contrast to the location of the peak contact pressure at central bottom on
the cartilage for the normal foot, it shifts to medial bottom for the severe HV foot, which may
aggravate the symptom of “painful bunion” which is one of the most common complaints
among HV patients [35]. Moreover, the component joint force in the medial-lateral direction
presented to be opposite between HV and normal foot. The severe HV foot shows lateral
reaction force at the first MTP joint during balanced standing, suggesting that loading of body
weight alone could predispose the patient to the risk of developing HV deformity.

4.4. Limitations
The FE models in this study were based on some simplifications and assumptions. First, the
bone was considered as homogeneous, isotropic, and linear elastic material. There is research
reporting that a difference in peak von Mises stress in the femur between isotropic and
anisotropic assignment was less than 1.2% under the loading conditions of double-leg standing.
As a result, it is feasible to consider the bone material as isotropic linear elastics, since this study was conducted under standing load. Additionally, cortical and cancellous bone were not defined, while the bone property was regarded as a weighted average of cortical and trabecular elasticity. Despite lack of validation, the value of elastic modulus (7300 MPa) has been adopted as foot bone material in the majority of studies [36]. Second, the geometry of body representing cartilage was not obtained from actual cartilage structures, as it is difficult to distinguish these in CT images. Third, this study created a representative single-subject model of a severe HV foot (HVA: 22.82°; IMA: 14.14°). Foot structure, such as arch height and toe deformity, may vary among HV feet; therefore, the presented data should be considered as a first rough approximation. Lastly, this study considered the skeletal structural difference (i.e., the different angle in Figure 1) as the major cause of mechanical changes. It should be noted that HV is also associated with hypermobility of the first metatarsophalangeal joint, which can be simulated through reducing elastic modulus of forefoot ligaments [11], while the material properties of all corresponding components were assumed consistent between the patient-specific model and the normal model in this study.

5. Conclusion

Internal stress is significant for better understanding of foot biomechanics as well as pathology of foot problems related to deformities. This study developed FE models of a normal foot and a severe HV foot to predict the internal metatarsal stress and MTP joint loading during balanced standing. Generally, increased von Mises stress at metatarsals and decreased joint loading at MTP were observed in the HV foot in comparison to the normal foot. Specific to the first MTP joint, the regions with high contact pressure of the severe HV foot exhibited a medial shift. Findings in this study suggest that load bearing may predispose patients to higher risk of metatarsal injuries and the functional impairment of the metatarsophalangeal joints. Further improvement of the FE foot model, including cortical and trabecular bones and inhomogeneous
property assignment, will be conducted to obtain more accurate predictions for better comparison.

Conflict of interest
None declared.

Acknowledgments
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Reference


Fig. 1. Hallux valgus angle (HVA) and intermetatarsal angle (IMA) for hallux valgus foot model (a) and normal foot model (b).

Fig. 2. The three-dimensional finite element model and the application of boundary and loading conditions.
Fig. 3. Comparison of the plantar pressure between experimental measurement (a, c) and computational prediction (b, d) in balanced standing position.

Fig. 4. Comparison of the von-Mises stress at five metatarsals between normal foot and hallux valgus foot.

Fig. 5. Comparison of contact pressure at metatarsophalangeal joints between normal foot and hallux valgus foot.

Fig. 6. Posterior view of contact pressure at the first metatarsophalangeal joint of normal foot (a) and hallux valgus foot (b). The red rectangles indicate the first MTP joint and the red circles indicate the regions with high pressure (Unit: MPa).

Fig. 7. Comparison of the resultant joint force at the first metatarsophalangeal between normal foot (F_N) and hallux valgus foot (F_S). X: Medial-Lateral direction (+: lateral; -: medial); Y: Anterior-Posterior direction (+: anterior; -: posterior); Z: Superior-Inferior direction (+: inferior; -: superior).
Table 1. Material properties and mesh element types for the foot model components.

<table>
<thead>
<tr>
<th>Component</th>
<th>Element Type</th>
<th>Young’s Modulus E (MPa)</th>
<th>Poisson’s Ratio ( \nu )</th>
<th>Cross-section Area (mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bone[19, 20]</td>
<td>Hexahedral solid</td>
<td>7300</td>
<td>0.3</td>
<td>-</td>
</tr>
<tr>
<td>Cartilage[16, 21]</td>
<td>Hexahedral solid</td>
<td>1</td>
<td>0.4</td>
<td>-</td>
</tr>
<tr>
<td>Ligaments[21, 22]</td>
<td>Tension-only spar</td>
<td>260</td>
<td>0.4</td>
<td>18.4</td>
</tr>
<tr>
<td>Plantar Fascia[21, 23]</td>
<td>Tension-only spar</td>
<td>350</td>
<td>0.4</td>
<td>58.6</td>
</tr>
<tr>
<td>Plate[21]</td>
<td>Hexahedral solid</td>
<td>17000</td>
<td>0.4</td>
<td>-</td>
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</tbody>
</table>
Table 2. The element type and coefficients of the hyperelastic material used for the encapsulated soft tissue.

<table>
<thead>
<tr>
<th>Element Type</th>
<th>C10</th>
<th>C01</th>
<th>C20</th>
<th>C11</th>
<th>C02</th>
<th>D1</th>
<th>D2</th>
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<tbody>
<tr>
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<td>0.08556</td>
<td>-0.05841</td>
<td>0.03900</td>
<td>-0.02319</td>
<td>0.00851</td>
<td>3.65273</td>
<td>0.00000</td>
</tr>
</tbody>
</table>
$F_N = 9.63 \text{N}$

$F_S = 4.93 \text{N}$
1. A severe hallux valgus FE models were constructed. 2. Pathological model predicted higher metatarsal stress and lower metatarsophalangeal pressure. 3. Severe hallux valgus is a potential risk of forefoot pain and functional impairment.