Effect of humidification of reactive gases on the performance of a proton exchange membrane fuel cell

Tabbi Wilberforce\textsuperscript{1}, O. Ijaodola\textsuperscript{1}, F.N. Khatib\textsuperscript{1}, E.O. Ogungbemi\textsuperscript{1}, Zaki El Hassan\textsuperscript{1}, James Thompson\textsuperscript{1}, A. G. Olabi\textsuperscript{2,3}

1. Institute of Engineering and Energy Technologies, University of the West of Scotland, United Kingdom
2. Dept. of Sustainable and Renewable Energy Engineering, University of Sharjah, P.O. 11 Box 27272, Sharjah, UAE
3. Mechanical Engineering and Design, Aston University, School of Engineering and Applied Science, Aston Triangle, Birmingham, B4 7ET, UK
Abstract

This work studies the impact of water formation on the performance of Proton Exchange Membrane Fuel Cells (PEMFCs). The work examines water management in PEM fuel cells both experimentally and theoretically.

Experiments are conducted using a one stack PEM fuel cell fitted with Nafion membrane to evaluate its performance using both dry and humidified hydrogen and air. Results obtained confirms the importance of fuel humidification in improving the performance of the fuel cell with all levels of humidification producing better performance than that obtained using dry hydrogen or dry air. Experiments using air with 50% relative humidity indicate drop in the fuel cell performance when comparing the results to those from air with 100% relative humidity.

The experimental data provides the basis to validate a computation fluid dynamics model for the fuel cell that is used to carry out further studies and conduct a parametric analysis of the fuel cell performance to examine the effects of flow plates designs, flow patterns such as parallel and counter flow and level of humidification on membrane water saturation, flooding, water management, reactants concentrations and overall cell performance by observing parameters such as membrane protonic conductivity, current density, cell voltage and power.

The CFD model studies and compares the use of air and oxygen in PEM fuel cells and the results show that for 100% relative humidity the performance obtained using pure oxygen is only marginally better than the one obtained when using air. This indicates that it is more beneficial to use air at the right conditions in PEM fuel cells given the cost of pure oxygen as the overall economic balance and the ease of use favour the utilisation of air.

Key words: Humidification, PEM fuel cell, Polarization curve, ANSYS,

1.0 Introduction.

The search for new alternative fuel sources continues due the environmental impacts of the use of fossil fuels and their non-sustainable nature as they are being continuously depleted [1]. The high efficiency of proton exchange membrane fuel cells has led researchers and the industry to consider it as a possible replacement of fossil fuel [2, 3]. Fuel cells are best described as electrochemical devices that generate power by means of electrochemical reaction of a fuel (hydrogen) and oxidant (air/oxygen) [4]. The environmental effects of the usage of fuel cells are among the key indicators of the viability of this useful technology [5]. They produce no
harmful gases and hence considered the future of the energy industry. They are considered as the future of the automotive industry and could also be useful in other stationary and portable applications [6]. There are different types of fuel cells and most of them are named according to the electrolyte being used [7]. The last decades have seen the introduction of the Alkaline fuel cell (AFC), Direct Methanol fuel cells (DMFC), Phosphoric Acid fuel cells (PAFC), Molten Carbonate fuel cells (MCFC), Solid Oxide fuel cells (SOFC) and the Proton Exchange membrane fuel cells (PEMFC). The use of Proton Exchange Membrane fuel cells is preferred as they operate at low temperatures ranging from 30°C to 70°C and have high power density and they are useful for fast start-ups and rapid response to fluctuating demands [8].

The electrolyte of PEM fuel cells is solid polymer which is in the form of solid proton conducting membrane that acts as the electrolyte.

The main parts of the fuel cell are the Membrane electrode assembly (MEA) and the bipolar plates [9]. The membrane electrode assembly is made up of a gas diffusion layer which is porous, a proton exchange membrane and a catalyst layer sandwiched between two plates [9]. The bipolar plate serves as the medium through which the fuel or oxidant travels to the MEA for the electrochemical reaction to occur. The bipolar plates often have different pattern of grooves of flow channels to supply the fuel cell with the gases at both the anode and the cathode. This clearly indicates that an effective design of the bipolar plate will have a direct implication on the performance of the fuel cell. This is because the effective distribution of the fuel and oxidant over the membrane surface and the diffusion to the catalyst layer will enhance the use of the catalyst active sites, which are often platinum catalyst atoms that are dispersed in a layer as part of the MEA. Again, the water management in the fuel cell will be highly improved as by product of the electrochemical reaction will easily exit the cell. Another advantage of an effective flow plate design is the enhanced efficiency of the collection of the electrons [9]. Several investigations have been conducted on the design of the bipolar plate as it contributes to 60 percent of the weight of the fuel cell as well as 30 percent of the entire cost of the fuel cell [10]. Pins, straight, double serpentine, serpentine, interdigitated channels designs are some of the bipolar plate’s configurations that have been investigated in recent years [11, 12]. The pin type flow channels and that of the interdigitated flow channel were also reviewed [13].

Atul and Ramana [14] and Tabbi et al [15] observed that one of the main challenges hindering the ability of a fuel cell to operate at its full potential is the flow channel design and this in turn
impact the commercial viability of the use and wide adoption of fuel cell worldwide. Gas
distribution evenly through the flow channels leads to 50% increase in the power density
according to an investigation carried out by Carton et al [6]. The by-product of the
electrochemical reaction in the fuel cell is often water and heat. In effect, dissipation of the by-
product out of the fuel cell will critically contribute to the performance of the fuel cell by
reducing the chances of flooding in the membrane. This phenomenon is likely to occur because
of portions of the membrane covered by water hence not contributing to the electrochemical
reaction. Sometimes the water is also collected in the Gas diffusion layer as well. The area on
the membrane that does not participate in the chemical reaction is referred to as a dead zone.
Drying of the membrane could also have a detrimental effect on the fuel cell as protonic
conductivity through the membrane would be reduced due to an increase in resistance in the
membrane hence leading to high ohmic losses. Another investigation carried out concluded
that the power output for interdigitated designs was 1.4 times higher compared to traditional
bipolar plate designs (Serpentine). They further argued that reducing the cross-sectional area
of the flow channel from 50.75% to 66.67% of traditional flow field designs will increase the
performance of the fuel cell appreciably [16]. Nguyen [17] also explored the impact of varying
physical conditions such as temperature, atmospheric pressure, humidity and stoichiometric
ratio on the performance of the fuel cell. The report also confirmed that the fuel cell can perform
better even at higher temperature provided the humidification temperature is increased as was
also reported by Tabbi et al. [2]. Another conclusion made was that when the fuel cell is being
operated at a higher current density, the effect of humidifying the reactant at both the anode
and cathode region would not influence the performance of the fuel cell in any way. Kazim et
al [18] also investigated the effect of the bipolar plate design on water management. The
research considered comparing 2 types of landing to channel ratio (1:1 and 2:2) with respect to
two different bipolar plate designs i.e. serpentine and interdigitated for two different areas
(25cm² and 70cm²). A conclusion was deduced that increasing the cross-sectional area of the
channel of the fuel cell reduced the power density. Manso et al [19] considered three
dimensional numerical model studies of the counter flow via the GDL for serpentine bipolar
plate [19]. The pressure drop was lesser for proton exchange membrane fuel cell without
counter flow when compared to that of counter flow. The implications of using varying channel
dimensions and configurations were investigated using Ansys by Dilip and Trung [20]. The
work established the best optimum channel width and channel depth to increase the
performance of the fuel cell. Effect of water management on the performance of the fuel cell
using serpentine and interdigitated flow channels was reported by Nguyen [17]. The
investigation exposed the fact that electro-osmotic drag and back diffusion were the main parameters that helped in the formation of water at the cathode region after the electrochemical reaction between the fuel and oxygen when the current density is high. The rate of water production is normally higher than the rate of its removal hence in the inner porous layers the water accumulates. Water flooding occurs when this happens, and the direct effect is a reduced output voltage or current from the fuel cell [21-27].

A 2-dimensional model developed based on Darcy equation for flow in porous media was also investigated by Cano et al [23].

The standard diffusion equation for transport in the GDL and the boundary conditions obtained from the Butler – Volmer equation were used to describe the physical phenomena occurring in the catalyst region of the PEMFC. The interdigitated bipolar plate design again performed better with the results from the mathematical model they derived showing current density three times that obtained from a traditional serpentine proton exchange membrane fuel cell [24]. Khazae and Sabadbanfan [25] reviewed the literature and studied the effect of the different kinds of flow channel designs including serpentine, straight parallel flow field, z parallel flow field, pin or meshed flow field as well as the interdigitated flow field.

Design of experiments techniques were used to investigate three different flow channel designs of fuel cells operating at low temperatures [22]. Carton and Olabi also studied three-dimensional flow through an open pore cellular foam material using Fluent CFD with varying humidification conditions [6].

A 3-dimensional numerical analysis on a radial flow patterned PEMFC was conducted by Shimpalee et al [28]. The effect of relative humidity with respect to flow field design of a rectangular PEMFC having cross sectional area of 24.8cm² was also investigated by Liu and Li [29] who studied the effect of flow pattern of the fuel and oxygen on the performance of the fuel cell. The work showed that increasing relative humidity increased the performance of the fuel cell with a serpentine flow plate design. Impact of the size of the bends in the serpentine flow channel has also been investigated [30 – 32]. The numerical study for determining the current density and the effect of dryness of the membrane on the performance of the fuel cell has all been carried out but there is little parametric studies on the effect of flow field designs on the water management and power output [33]. Optimization of the flow channel for the anode and cathode flow regions is recommended to develop better understanding of water management in a fuel cell to prevent the possibility of the membrane flooding and also to ensure
optimal pressure drop through the flow channels. Detailed information about the fluid
dynamics for each humidification parameters considered was equally discussed. Many
researchers used CFD in analyzing their design concepts [34 – 39].
This work investigates the performance of a fuel cell with an active area of 25cm$^2$ numerically.
The work optimizes the said PEM fuel cell performance with respect to water management in
the membrane and the overall performance of the fuel cell at different humidification
conditions. This will improve the economics of the use of fuel cells by reducing the operational
cost of fuel cells at varying operational conditions and ensuring performance at peak levels.

2.0 Model Validation

The computational results generated in Ansys Fluent (shown in appendix A) were first
compared with experimental results obtained from the experimental setup shown in Appendix
B and those obtained by Cheng et al.[40]. There is a perfect agreement between the numerical
results generated in Ansys and those obtained in the laboratory as well as the results of Cheng
et al. [40] as shown in Fig. 1. The differences between the current densities of the three results
being compared are small and the standard deviation is less than 0.0075A/cm$^2$ which is smaller
than those obtained by Giri and Bannerjee (1975) [41].
Fig. 1. Numerical verification of the current density of the PEM fuel cell

The same observation can be said of Fig. 2, where the differences between power density curves for the three results were also small. Table 1 shows the specific voltage and current density obtained as well as the deviation between the experimental and computational results. The experimental results obtained showed lower values than the numerical/computational results as this can be attributed to experimental physical operating parameters like the cell operating temperature that kept fluctuating in the laboratory.
Fig. 2: Numerical verification of the Power density of the PEM fuel cell

Table 1: Comparison between computational and experimental data

<table>
<thead>
<tr>
<th>No.</th>
<th>Voltage (V)</th>
<th>Experimental results</th>
<th>Computational</th>
<th>Percentage Deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>0.90</td>
<td>0.0010</td>
<td>0.0015</td>
<td>0.66</td>
</tr>
<tr>
<td>b</td>
<td>0.85</td>
<td>0.05528</td>
<td>0.05429</td>
<td>1.80</td>
</tr>
<tr>
<td>c</td>
<td>0.80</td>
<td>0.08551</td>
<td>0.09001</td>
<td>4.99</td>
</tr>
<tr>
<td>d</td>
<td>0.75</td>
<td>0.1941</td>
<td>0.18510</td>
<td>4.60</td>
</tr>
<tr>
<td>e</td>
<td>0.70</td>
<td>0.2755</td>
<td>0.2801</td>
<td>1.64</td>
</tr>
<tr>
<td>f</td>
<td>0.65</td>
<td>0.3489</td>
<td>0.3378</td>
<td>3.18</td>
</tr>
</tbody>
</table>
2.1 Effect of the direction of the flow of the gas.

The first numerical simulation that was done was to determine the pattern of the flow of the gas as this will have a large impact on the performance of the fuel cell. Two types of flow patterns were considered, namely, parallel and counter flow patterns. Each of these flow patterns were considered for one specific geometry as shown in Fig. 3.

Fig. 3: PEM fuel cell geometry used in the simulation.
Fig. 4: Flow directions in the PEM fuel cell module a) Parallel flow b) Counter flow.
The counter/cross flow pattern (Fig. 4b) results in the gases moving in opposite direction to each other and in the parallel flow (Fig. 4a) arrangement all the gas flows in the same direction. It is also possible to design the flow channel for both the hydrogen and oxygen to flow in different (mixed) direction.

### 2.1.1 Parallel flow pattern

Concentration of hydrogen

This flow direction as shown in Fig. 4a allows the gas to be evenly distributed at the anode region of the fuel cell while at the cathode region the oxygen gas is also evenly distributed. It must be noted that a good distribution of the gas in the flow channel often leads to more current being generated by the fuel cell. It also supports the life span of the fuel cell as it aids in the water management of the cell.

Fig. 5 shows the hydrogen concentration at the anode region. The concentration of the hydrogen gas in Fig. 5 drops gradually between the inlet and the outlet indicating that the hydrogen is consumed as it flows from the inlet to the outlet of the anode flow field.

![Fig. 5: Hydrogen mass fraction in the anode region of the fuel cell](image)

The flow of the gas from the inlet to the outlet using this approach facilitates easy consumption of the hydrogen gas in the catalyst layer producing the electrons (e⁻) and protons (H⁺).
Concentration of oxygen

Oxygen gas is introduced to the fuel cell through the cathode region and it often comes either as pure oxygen or air. The drop in concentration of the oxygen at between the inlet and outlet indicates the consumption of the oxygen as it passes the cell in this flow channel direction. The ionised oxygen atoms react with the hydrogen ions released from the anode region of the fuel cell to form water which is the by-product of the electrochemical reaction. Fig. 6 shows oxygen mole fraction contour in the cathode region of the fuel cell which has 12 oxygen flow channels.

Fig. 6: Oxygen mole fraction contour in the cathode region of the fuel cell

Water concentration through the entire flow channel

The hydrogen diffuses from the anodic electrode to the cathodic electrode of the PEMFC. The hydrogen ions then react with the oxygen atom at the cathodic electrode leading to the formation of water and the electrons then flow through an external circuit.
Fig. 7: Water concentration through the anode region of the fuel cell

It is observed as shown in Fig. 7 that the largest amount of water will be produced in the mid region because that is where the electrochemical reaction will occur, and the water observed at the anode region is due to the fact that the hydrogen gas is 20% humidified. A careful examination of Fig. 7 also shows that the water concentration increases from the inlet to the outlet. The outlet water content is lower than the inlet indicating that a good amount of water will be removed from the fuel cell even though the building up of the water often start right from the inlet and increase to the outlet.

Protonic Conductivity

The structure as well as membrane hydration has a huge influence on the performance of PEMFCs as it determines the efficiency of the transport of the protons to the cathode region of the membrane.

Fig. 8 shows the protonic conductivity of the protons through the membrane. The protonic conductivity is usually expected to be uniform throughout the membrane indicating the availability of all regions of the membrane for electrochemical reaction to occur which leads to power density and output power increases.
Fig. 8: Contours of protonic conductivity through the membrane of the fuel cell

2.2 Effect of Counter flow

The cross/counter flow often leads to more current being generated by the fuel cell due to preferential arrangement of the reactive gases moving opposite to each other. As shown on Fig. 9b, the current flux density obtained for the 2 flow directions indicates that more current will be generated if the cross/counter flow arrangement is used.
Fig. 9: Comparison between a) counter and b) parallel flow direction.

The polarization curves shown in Fig. 10 and Fig. 11 were used to determine the best flow directions for the rest of the simulations [39]. By analyzing the polarization curves shown below, it becomes clear the counter flow pattern resulted in better performance in terms of power and current density. It showed almost 9.5% increase in the overall current generated when compared to the parallel flow directions. With the active area of the fuel cell under investigation being 25cm², and the cell voltage kept at 0.6V, the current density obtained using the parallel flow was 0.389A/cm² and the corresponding power density was 0.2334 W/cm but the current density for the same constant cell voltage of 0.6A/cm² using a counter flow direction gave the current density and power density as 0.451A/cm² and 0.2706, respectively, clearly showing the positive impact of the fluid flow pattern on the characteristic performance of PEMFCs.
Fig. 10. Polarization curve for the parallel and counter flow direction

Fig. 11. Polarization curve for counter and parallel flow
2.3 Effect of hydrogen gas humidification on the performance of the fuel cell

The by-product of the electrochemical reaction in the fuel cell is water as explained earlier hence it is common for researchers not to humidify the reactive gases to avoid contributing to the flooding of the cell as this will lead to some portions of the active catalyst area become covered with water resulting in reduction of the performance of the fuel cell.

The counter flow arrangement was used in the subsequent simulations discussed below. A constant cell voltage of 0.95 was maintained for simulations using dry hydrogen and humidified hydrogen as well as dried oxygen and humidified oxygen. Each of these parameters were varied systematically to determine the impact of each parameter on the overall performance of the fuel cell.

Fig. 12: Current flux density magnitude contours of humidified hydrogen gas through the anode bipolar plate (amps/m²)
Fig. 12 shows the current flux density profile for a humidified hydrogen gas through the proton exchange membrane fuel cell.

It can also be observed that the fuel cell generates more current if the anode reactive gas is humidified as compared to using a dry hydrogen gas as shown in Fig 13. The main rational for the occurrence of this phenomenon is because the membrane close to the anode becomes dehydrated when dry hydrogen gas is used as compared to the use of wet or humidified hydrogen gas. The dehydration increases the resistance in the cell (electrolyte) reducing the release of electrons through the externally connected circuit.

Fig. 13: Current flux density magnitude for dry hydrogen gas (amps/m²)

Fig. 14 also shows the mass fraction contour for both the humidified hydrogen and dry hydrogen. As expected due to the hydrogen gas being humidified in Fig. 14a, some of the area is occupied by the hydrant (water) throughout the entire flow channel compared to the dry hydrogen where the space above the membrane is predominantly hydrogen. Also in the latter case, more hydrogen gas will flow through each channel arm compared to the humidified gas, the dearth of water in the gas stream leads to reduced membrane humidification and increased resistance to proton movement with negative impact on the overall performance of the cell.
Fig 14: Mass fraction of hydrogen a) humidified b) dry hydrogen

Membrane water concentration

A good amount of humidification of the membrane as captured in Fig. 15 is required in order for the protons conductivity through the membrane to be highly efficient. Using 100% dry hydrogen gas will make the membrane dry reducing the transport of the hydrogen ions through the membrane. This is one of the important reasons for the performance of PEMFCs being very low when pure dry hydrogen is used.
Fig. 15. Membrane protonic conductivity (V) a) humidified b) dry hydrogen

Overpotential

The overpotential through the fuel cell for both humidified and dry hydrogen gas was also studied and from Fig. 16. It can be seen that the loss due to using dry hydrogen is higher when compared to using a humidified hydrogen gas.

Fig. 16: Membrane over potential (v) for dry and humidified hydrogen gas.

The polarization curves of Fig. 17 show that the limiting current density when using a humidified hydrogen gas occurs slower than when using a dry hydrogen gas. This occurs
because the losses when a dry gas is used are always greater than when using a humidified hydrogen gas. A fuel cell cannot produce any current greater than its limiting current value hence using the dry hydrogen gas yields small amount of current from the fuel cell.

![Cell Voltage vs Current Density](image1)

**Fig. 17:** Comparison of the effect of using dry hydrogen and humidified hydrogen gas

The same can be said of the power density curve shown in Fig. 18 where the humidified hydrogen gas performs better than the dry gas.

![Power Density vs Current Density](image2)
2.4 Effect of humidification of the oxygen gas at the cathode region.

Since the need for the hydrogen to be humidified is confirmed, the investigation progressed to determine the effect of oxygen humidification or air humidification on the performance of a fuel cell and which of the two will be the better option to improve the characteristics performance of any PEMFC. The major challenge that determines the performance of most fuel cells in general is how the by-product which is water can be removed effectively out of the fuel cell while keeping the membrane kept properly humidified.

The overpotentials are affected by the water content in the fuel cell and dehydration or too much water in the fuel cell can all have adverse effects on the overall performance of the fuel cell. For good protonic conductivity, the membrane is recommended to be properly humidified. Protonic conductivity reduces in instances where the membrane is not well humidified thus increasing the cell resistance and activation overpotentials therefore increases due to the membrane drying out. Too much water will also impede the reactant transport to the active catalyst layer for electrochemical reaction to occur and this situation increases the diffusion overpotential. One proactive way of maintaining the membrane constantly hydrated is through the humidification of the oxygen gas as well. The humidification of the oxygen gas is also dependent on the gas temperature, pressure, channel design and the thickness of the membrane.

The current density generated usually defines the amount of water produced by the fuel cell. Fig. 19 shows the water transport process through a fuel cell.
Fig. 19: Transport processes in Fuel cell

Whenever a load is placed on the fuel cell electro-osmotic transport process occurs. As the hydrogen ions flow through the polymer from the anode to the cathode, they carry water molecules with them. The number of water molecules that the hydrogen ions carry along on average is called the electro-osmotic drag coefficient.

Water diffusion through the membrane occurs when the concentration gradient in the cathode push the water through the membrane and this process is called the back diffusion. Water accumulation at the cathode region which normally leads to flooding of the fuel cell if not carefully checked is caused by these two processes: electro-osmotic drag and back diffusion. The water formed at the cathode can be removed from the PEMFC through the flow channels. Another method of removing water is by using the reactant gases. Some reactant gases carry the by product (water) along as they flow through the fuel cell especially when they are under saturated or flowing at high rates. The efficiency of water removal also depends on the operating conditions such as temperature, pressure and gas flow rates.

For this investigation, the simulations were carried out using Air with 100% relative humidity (RH), Air with 50% RH and dry oxygen and the simulation results were compared with those obtained experimentally.
2.5 Performance of a fuel cell with 100% RH of Air

As with the increase in the humidity of the hydrogen gas, 100% RH of air showed a better fuel cell performance as shown in Fig. 20 when compared with dry and lower RH values. This is because the humidified air did not strip the membrane of water and prevented it from becoming dry thus help protonic conductivity and also increased electro osmotic drag and back diffusion. These factors helped keep the fuel cell operating at its maximum potential.

Fig. 20. Current flux density magnitude on the current collector with 100% RH of Air

Fig 21 shows the water contours in the membrane which indicate that the membrane contains good amount of water which will facilitate the transport of the protons increasing the performance of the fuel cell. As the by-product of the electrochemical reaction is water, the operating cell temperature must be kept high to aid in the easy removal of the product water through vaporization to reduce the risk of flooding.
Fig. 21: Membrane water content

2.6 Performance of a fuel cell with 50% RH of Air

The performance of the fuel cell with 50% RH Air is slightly lower than that with 100% RH Air as shown in Fig. 22 and the fuel cell can still give good amount of current even with 50% RH Air. As before, the cell operating temperature and the flow rate of the gas should be kept at optimum conditions to reduce the possibility of the fuel cell drying out.
Since the relative humidity of the air is only 50%, the membrane loses water to the air resulting in lower water contents in the membrane (Fig. 22) with corresponding reduction in the protonic conductivity of the membrane. This in turn reduces the flow of protons implying lower current density fluxes as shown in Fig. 23. This increased resistance contributes to the reduced performance of the fuel cell when compared to the cell using 100% humidified Air.
2.7 Performance of a fuel cell using dry Oxygen

As expected, the use of dry oxygen will have a negative effect on the fuel cell as can be seen from the current flux density magnitude contours obtained from the dry oxygen on the current collectors as shown in Fig. 24 and the amount of current obtained was very low compared with the other simulation results with higher RH.
An important factor that contributes to the reduction in the performance of PEMFC using dry oxygen is poor back diffusion at the cathode region of the fuel cell due to the membrane being dry when the dried oxygen was introduced to the cell as could be seen in Fig. 25. Even though the electro osmotic drag experienced at the anode region will maintain some amount of moisture in the membrane, the dry oxygen impacts the back-diffusion characteristics of the fuel cell and reduces the performance of the fuel cell in general. With the membrane not being adequately hydrated, the protonic conductivity of the fuel cell will also be reduced as shown in Fig. 26. The low protonic conductivity will also contribute further to the fuel cell not performing properly.
Fig. 25: Membrane water content of the fuel cell using dry oxygen a) anode region    b) Cathode region

Fig. 26: Protonic potential of the fuel cell using dry oxygen gas
2.8 Performance of the fuel cell using 100% RH oxygen

Using 100% RH oxygen showed high performance characteristics very similar to those obtained using air with 100% RH humidity.

This work validates the previous postulated hypotheses to explain the high performance of using humidified oxygen as shown by the contours obtained from the current flux density magnitude plots shown in Fig. 27.

Another reason for the high performance of the fuel cell using humidified oxygen is the easy flow of protons from the anode to the cathode due to high membrane hydration as shown in Fig. 28. Once the membrane is well humidified with a good cell operating temperature, the fuel cell will perform better at its peak.
Fig. 28: a) Membrane water content b) Protonic conductivity using humidified oxygen.

Fig. 29 and Fig. 30 shows the polarization curve for comparing the various humidification conditions used in this investigation as well as the power density plots for each conditions, and these are compared with experimental results. It can be observed that the 100%RH oxygen performed better followed by the 100%RH Air and the 50%RH Air.

Fig. 29: Polarization curve of the performance of the fuel cell with respect to current density and voltage.
Fig. 30. Polarization curve for PEMFCs with respect to current density and power density

Given the closeness of the results, and due to the cost of operating fuel cell using pure humidified oxygen, most researchers prefer using humidified air as it is readily available and abundant.

3.0 Conclusion

This work presents both experimental and theoretical analysis of the performance of PEMFCs with respect to water formation and water management.

The experimental study used hydrogen and air and examined the performance with and without humidification and in all cases the results showed that humidification produced better overall performance in the fuel cell. Results obtained from 100% relative humidity of hydrogen and air are slightly better than those for 50% relative humidity indicating that dryer fuel or air result in water stripping from the membrane leading to increased protonic transport resistance and lower overall cell performance. This gives strong indication that to achieve the optimum performance from a PEM fuel cell, the proper level of humidification must be used to strike a balance between avoiding cell flooding and minimising protonic transport resistances.
Experimental results from this study and from the literature were used to validate a newly developed CFD simulation model which was then used to conduct parametric studies to examine the effect of several operating parameters on the PEM fuel cells overall performance. The results showed that the process of water management and overall fuel cell performance is strongly impacted by the design of the fuel cell flow plate.

Simulation with 100% relative humidity of oxygen and air showed that the use of pure oxygen provided slightly better results but they are not enough to justify the replacement of air by pure oxygen given its cost and the ease of the use of air which is readily available and requires minimal technical changes in the design of the fuel cells. Flow rate of gases and their flow patterns also play important role in the improvement of the process of water management and the overall fuel cell performance.
Reference


[39]. T. Wilberforce, A. Al Makky, A. Baroutaji, R. Sambi and A.G Olabi, Optimization of bipolar plate through computational fluid dynamics simulation and modelling using nickle
open pore cellular foam material, International conference on renewable energies and power quality (ICREPQ’17), ISSN 2171-038X, No 15 April 2017


### Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varphi$</td>
<td>Rate of change quantity</td>
</tr>
<tr>
<td>$\Phi$</td>
<td>Momentum</td>
</tr>
<tr>
<td>$V$</td>
<td>Volume</td>
</tr>
<tr>
<td>$T_\varphi$</td>
<td>Diffusivity coefficient</td>
</tr>
<tr>
<td>$S$</td>
<td>Source term</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Mixture viscosity</td>
</tr>
<tr>
<td>$k$</td>
<td>Catalyst and GDL permeability</td>
</tr>
<tr>
<td>$k_{\text{eff}}$</td>
<td>Effective conductivity</td>
</tr>
<tr>
<td>$h_i$</td>
<td>Species enthalpy</td>
</tr>
<tr>
<td>$j_i$</td>
<td>Species flux density</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Electrical conductivity</td>
</tr>
<tr>
<td>$\Phi_{\text{mem}}$</td>
<td>Membrane phase potential</td>
</tr>
<tr>
<td>$\Phi_{\text{sol}}$</td>
<td>Solid phase potential</td>
</tr>
<tr>
<td>$j_{\text{ref}}$</td>
<td>Reference exchange current density</td>
</tr>
<tr>
<td>$\zeta$</td>
<td>Specific active surface area</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Concentration dependence</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Transfer coefficient</td>
</tr>
<tr>
<td>$F$</td>
<td>Faradays constant</td>
</tr>
<tr>
<td>$[A]$</td>
<td>Molar concentration of reactant at anode</td>
</tr>
<tr>
<td>$[C]$</td>
<td>Molar concentration of reactant at cathode</td>
</tr>
<tr>
<td>$\lambda_m$</td>
<td>Membrane water content</td>
</tr>
<tr>
<td>$T_{\text{cell}}$</td>
<td>Cell temperature</td>
</tr>
<tr>
<td>$\Pi$</td>
<td>Local species overpotential</td>
</tr>
<tr>
<td>$V_{\text{OC}}$</td>
<td>Open circuit voltage</td>
</tr>
<tr>
<td>$p_u$</td>
<td>Upstream pressure</td>
</tr>
<tr>
<td>$p_d$</td>
<td>Downstream pressure</td>
</tr>
<tr>
<td>$k_{an}, k_{ca}$</td>
<td>Nozzle constant</td>
</tr>
<tr>
<td>$F_{an}$</td>
<td>Input flow rate at anode</td>
</tr>
</tbody>
</table>
\( P_{an} \) \hspace{1cm} \text{total pressure in anode}
\( P_{sat} \) \hspace{1cm} \text{Saturated vapour pressure}
\( P_{H_2O.an} \) \hspace{1cm} \text{Water vapour pressure at anode}
\( P_{ca} \) \hspace{1cm} \text{total pressure in cathode}
\( P_{H_2O.ca} \) \hspace{1cm} \text{Water vapour pressure at cathode}
\( V_{an} \) \hspace{1cm} \text{Volume of anode}
\( V_{ca} \) \hspace{1cm} \text{Volume of cathode}
\( F_{ca} \) \hspace{1cm} \text{Input flow rate at cathode}
Appendix A: Numerical Modelling.

The simulation process was conducted in four stages. In the first stage a model geometry of the fuel cell was created using Solid Works 2016 then saved in Parasolid format.

In the second stage a mesh was generated using ANSYS ICEM CFD. The various layers in the fuel cell were carefully defined in the mesh and the boundary conditions for each of the 9 layers in the fuel cell were properly defined. Also the inlet and outlet boundary conditions of the geometry were defined in the software. The flow direction was carefully identified as any discrepancy in the flow direction will prevent the convergence of the calculations. The operating cell temperature and pressure were also specified.

In the third stage, the ANSYS Fluent solver is used to all the governing equations that represents the conservation of mass, momentum and energy in the Cartesian plane (x,y,z), as well as the equations that account for electrochemical reactions, currents and the species taking part in the reactions.

The last stage is post processing where the results obtained from the simulation were processed to provide the necessary information for the analysis. These include current density, power density, species concentrations (hydrogen, oxygen and water), protonic conductivity and the pressure drop in the fuel cell that aid in the analysis of the performance of the PEM fuel cell.

Design of the Geometry:

The geometry was created using Solid Works 2016 as explained earlier. The geometry has nine layers in all representing the entire single stack fuel cell. These layers were initially created as a 2D diagram then converted to 3D using the extrude command in Solid Works. All the nine layers were then assembled together using the mating command. The nine layers are the anode current collectors, anode channel, anode diffusion layer, anode catalyst layer, membrane, cathode catalyst layer, cathode diffusion layer, cathode Channel and cathode current collector. Fig. A1 shows one of the assembly layers in solid works.
Fig. A1: Exploded View of Fuel Cell Assembly with Round Serpentine Flow Plate Design in Solid Works
The various dimensions for each layer are clearly specified in Table A1. The serpentine design that was used during the simulation was made up of a single channel just like what is on the market to clearly differentiate the effect of each of the humidification condition on the fuel cell performance.

Table A1. The dimensions for the modelled PEMFC

<table>
<thead>
<tr>
<th>Layers</th>
<th>Dimensions</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thickness of the membrane</td>
<td>0.05</td>
<td>mm</td>
</tr>
<tr>
<td>Catalyst layer thickness</td>
<td>0.15</td>
<td>mm</td>
</tr>
<tr>
<td>Gas diffusion layer thickness</td>
<td>0.5</td>
<td>mm</td>
</tr>
<tr>
<td>Width of the flow channel</td>
<td>1.99</td>
<td>mm</td>
</tr>
<tr>
<td>Land to width</td>
<td>1.99</td>
<td>mm</td>
</tr>
<tr>
<td>Width of the current collector</td>
<td>2</td>
<td>mm</td>
</tr>
<tr>
<td>Inclination</td>
<td>5</td>
<td>deg</td>
</tr>
</tbody>
</table>

Meshing of the Geometry

One of the key conditions that would aid in confirming the validity of the simulation results is the quality of the mesh. An improperly meshed geometry will not simulate the geometry and the system behaviour accurately.

The mesh was developed by considering each layer separately as they have different dimensions particularly with the thickness and channel length. Using the blocking method, each layer is meshed separately. This approach allowed for better definition of the mesh elements shapes and sizes allowing for the creation of hexahedral elements to better define the mesh to capture the thermal and hydraulic behaviour of the fuel cell as well as the electrochemical reactions. Mesh independency, or convergence tests, were then performed to ensure that the model results are independent of the number or size of the elements of the grid. The initial mesh tests had 2015321 elements, 2517821 elements and 3010212 elements. It was observed that above 2,517821 the results were grid independent. The voltage difference obtained as the mesh elements increased
above 2517821 was less than 1% as can be seen in Fig. A2. The mesh convergence studies were repeated for all the designs used in this study. The discretization of the cells was also done using ICEM CFD for building the unit cells. The simulation of PEMFCs is complex and requires the computational grid elements to be of very good quality if reliable results is to be obtained. This is also important as it impacts on solver stability during the solution process [34] and the computational resources required to achieve convergence and better accuracy.

Fig. A2. Types of mesh applied to simulation.

It is commonly believed that an increase in the number of elements (fine mesh) implies that the results generated will be of better accuracy but this approach requires large resources to carry out the simulations. A more efficient approach is to refine the mesh using the tools providing in the meshing software to obtain better quality cells and mesh and to strike a good balance between the acceptable level of accuracy and the necessary computational time. It is therefore imperative that grid independent analysis is properly conducted to ensure the validity of the simulation results. The histogram of Fig. A3 shows that above 2500000 elements the current being generated was the same for a cell voltage of 0.4.
Fuel Cell Mathematical Model:

A fuel cell is an energy conversion device used for the conversion of the chemical energy in fuel(s) directly into electrical energy. The fuel cell has the triple-phase boundary condition referred to as the catalyst layer. Fig. A4 shows the schematic diagram of a typical configuration of PEM fuel cell as illustrated in ANSYS Fluent 15.0 Fuel Cell module manual [39]. The computational fluid domain is also made up of the ionic conducting electrolyte. From Fig. A3, it can be seen that the flow of hydrogen into the fuel cell occurs via the anode region. The anode region reactive gas then diffuses through the pores of the GDL before reaching the catalyst active sites of the fuel cell. On reaching the catalyst, it dissociates into protons and electrons with the former flowing through the membrane towards the cathode region and the electrons flowing through an external load circuit producing the current. The electrons then flow from the anode electrode, via the current collectors and GDL to the cathode. Hydrogen ions, electrons and oxygen then combine at the cathode forming water.
Fig. A4. Diagram of a proton exchange membrane fuel cell [39]

Two electric potential fields are solved in fuel cell Ansys Fluent. One of the potentials is mathematically computed in the electrolyte as well as the catalyst layer whiles the other computation is solved for the catalyst layer, the electrode being porous in nature and current collectors. The determination of rate of electrochemical reaction is solved in the catalyst region.

By varying the electric potential for the cathode region whiles grounding that of the anode region to zero, the current density value can easily be computed. Similarly, it is possible to determine the cell voltage by specifying the cell current. Eqn. A1 and Eqn. A2 show the triple phase boundary layers (TPB) for the anode and cathode.

\[ H_2 \leftrightarrow 2H^+ + 2e^- \quad (Anode \ Triple \ phase \ boundary) \]  

\[ \frac{1}{2}O_2 + 2e^- + 2H^+ \leftrightarrow H_2O \quad (Cathode \ Triple \ phase \ boundary) \]  

Electrons flow through the external circuit to the cathode while the protons (H\(^+\)) diffuse through the membrane from the anode triple phase boundary to the cathode triple phase boundary creating electrical circuit. Water vapour pressure exceeds the saturation pressure producing liquid water as excess water is produced around the cathode region at high current densities due to osmotic drag,
back diffusion and the electrochemical reaction occurring on the porous catalyst layer in the fuel cell. The transport of water away from the cathode region is very important as it impacts the performance of the fuel cell.

Electrochemistry modelling.

Using fluent 15.0 all the governing equations were solved for the modelled proton exchange membrane fuel cell. Double precision serial processing is used in Fluent and model, steady laminar flow was assumed. The fuel cell being an add-on package in ANSYS was introduced to integrate fluid dynamics equations and the electrochemical equations in Ansys Fluent. The Navier-Stokes equations (Eq. A3) describing the 3-dimensional fluid flow in the cell were solved in Fluent using turbulence modelling to obtain approximate solutions. Similar approaches were used to treat heat transfer and electrochemical reactions.

\[
\frac{\partial}{\partial t} \int p \varphi dV + \oint p \varphi V \cdot dA + \oint T_\varphi \nabla \varphi \cdot dA = \int S_\varphi dV \tag{A3}
\]

The conservation equation explains how the rate of change of a quantity \( \varphi \) in a control volume plus transport due to convection and species diffusion in and out of the control volume are the source term. The quantity transported (energy, momentum) is \( \varnothing \), \( t \) is time, \( A \) is area of the surface, \( V \) is the volume, \( T_\varphi \) is the diffusivity coefficient, \( S \) is source term. Mass conservation which factors in the fluid streamline, mass dispersion and electrochemical responses were taken into consideration and incorporated into the continuity equation. The continuity equation is shown as Eqn. A4.

\[
\nabla (\bar{V}) = S_m \tag{A4}
\]

Where \( S_m \) is the species sources term and \( \bar{V} \) is the fluid velocity vector.

Eqn. A5 shows steady state flow momentum equation:

\[
p \frac{\bar{V}}{d\bar{t}} = -\nabla p + \mu (\nabla^2 \bar{V}) + S_p \tag{A5}
\]

where \( \mu \) is mixture viscosity, \( p \) the static pressure, \( \rho \) is the density and \( S_p \) is source term which is given by:
\[ S_p = -\left(\frac{\mu}{k}\right) \]  \hspace{1cm} (A6)

where \( \mu \) is the gas velocity, \( k \) is the catalyst layer and GDL permeability, \( \vec{V} \) is the superficial velocity.

The equation for the energy is also solved using the steady state energy equation as shown in Eqn. (A7).

\[ \nabla \cdot \left[ \vec{V}(\rho_t + p) \right] = \nabla \left( k_{eff} \nabla T - \sum_i h_i \vec{J}_i \right) \]  \hspace{1cm} (A7)

The total energy is represented by \( E \), \( k_{eff} \) is the effective conductivity, \( h_i \) is species enthalpy and \( J_i \) is species flux density. Species transport equation also considered mass conservation for the type of gas to focus on the mass fraction of each of the species \( y_i \). Eqn. A8 shows the species transport equation.

\[ \nabla \cdot (\rho \vec{V} y_i) = -\nabla \vec{J}_i + S_i \]  \hspace{1cm} (A8)

The source term of the species is represented by \( S_i \) and \( \vec{J}_i \) is the species flux density. Since the fluid flow through the flow field is laminar, diffusion is given by:

\[ \vec{J}_i = -p D_i \cdot \nabla y_i \]  \hspace{1cm} (A9)

\[ h_i \vec{J}_i = -p D_i \cdot \nabla y_i \]

where \( D_i \) is the diffusion coefficient for the species \( i \).

The following assumptions were made prior to the simulations. All the reactant gases are assumed to behave as ideal gases.

- Fluid flow is assumed to be incompressible, laminar and steady.
- The temperature was maintained at 353K for all the simulation work.
- The isotropic porous zones considered during the simulation were the catalyst layers, GDL and the electrolyte.
- The active region where electrochemical reaction occurred was also considered as the TPB or the catalyst layer.
- Gravitational effects were negligible.
- Transfer of water through the electrolyte was as a result of back diffusion and electroosmotic drag only.

Fig. A5 shows the boundary conditions for the electric potential in PEM FC. The computation of the rates of the anodic and cathodic reactions is the main challenge with the electrochemical simulations. The surface potential is the main driving force behind these reactions. The surface potential is simply the difference between the phase potential of the solid and the phase potential of the electrolyte/membrane. Two equations are solved for the fuel cell model. The first equation (Eqn. A10) accounts for electrons ($e^-$) transport through the solid conducting materials such as the current collectors and solid grids of the porous media, while the other potential Eqn. (A4) represents the protonic transport of $H^+$ and $O_2^-$. 

Fig. A5: Boundary conditions for the Electric potential (Solid Membrane)[40]
\[ \nabla \cdot (\sigma_{sol} \nabla \phi_{sol}) + R_{sol} = 0 \] (A10)

\[ \nabla \cdot (\sigma_{mem} \nabla \phi_{mem}) + R_{mem} = 0 \] (A11)

where \( \sigma \) represents the electrical conductivity (1/ohm-m), \( \phi \) represents the electric potential (Volts), \( R \) represents the volumetric transfer current (A/m\(^3\)).

Two types of external boundary exist. The first is those that have electrical current flowing through them and boundaries where current do not flow through them. There is virtually no loss of an ionic current in the PEMFC via the boundary externally, hence the external surface boundary conditions for the membrane phase potential \( \phi_{mem} \) is zero indicating no exchange through the external boundaries. The solid phase potential \( \phi_{sol} \) has external boundaries for anode and cathode electrode connected directly to the external electric circuit and it is through these boundaries that the current produced by the PEMFC passes. Fixed values were set for the \( \phi_{sol} \) (potentiostatic boundary conditions). The anode boundary condition is usually set to zero and the cathode boundary condition is positive and this is the cell voltage. In situations where a constant flux is specified in the cathode region, this means specifying galvanostatic boundary conditions. The current transfer is non–zero for the catalyst layers.

Solid phase, \( R_{sol} = -R_{an} (< 0) \) for the anodic electrode and \( R_{sol} = +R_{cat} (> 0) \) for the cathodic electrode. Membrane phase, \( R_{mem} = +R_{an} (> 0) \) for the anodic side and \( R_{mem} = -R_{cat} (< 0) \) for the cathodic electrode. Current density can also be calculated further using the butler volmer equation as shown in Eqn A12 and A13 for the anode and cathode respectively.

\[ R_{an} = (\zeta_{an})^{ref}_{an} \left( \frac{[A]}{[A]_{ref}} \right)^{Y_{an}} \left( e^{\alpha_{an}F\eta_{an} / RT} - e^{-\alpha_{cat}F\eta_{an} / RT} \right) \]  
[ A12 ]

\[ R_{cat} = (\zeta_{cat})^{ref}_{cat} \left( \frac{[C]}{[C]_{ref}} \right)^{Y_{cat}} \left( -e^{+\alpha_{an}F\eta_{cat} - RT} - e^{-\alpha_{cat}F\eta_{cat} / RT} \right) \]  
[ A13 ]
where \( j^{\text{ref}} \) is the reference exchange current density for the active surface area (A/m\(^2\)), \( \zeta \) is the specific active surface area (1/m), \([\cdot]\) and \([\cdot]_{\text{ref}}\) indicate local species concentration and reference value (kmol/m\(^3\)), respectively. \( \gamma \) is concentration dependence \( \alpha \) is the transfer coefficient (dimensionless) and \( F \) is Faraday's constant (9.65 x 10\(^7\) C/kmol).

The Tafel formula is the simplified version of the Butler-Volmer equation and is shown in Eqn. A14 and A15.

\[
R_{\text{an}} = (\zeta_{\text{an}} j_{\text{an}}^{\text{ref}}) \left( \frac{[A]}{[A]_{\text{ref}}} \right)^{\gamma_{\text{an}}} (e^{\alpha_{\text{an}} F \eta_{\text{an}} / RT}) \quad \text{[A14]}
\]

\[
R_{\text{cat}} = (\zeta_{\text{cat}} j_{\text{cat}}^{\text{ref}}) \left( \frac{[C]}{[C]_{\text{ref}}} \right)^{\gamma_{\text{cat}}} (-e^{+\alpha_{\text{an}} F \eta_{\text{cat}} / RT}) \quad \text{[A15]}
\]

To accurately calculate the transfer currents inside the catalyst layers in fuel cells, ANSYS Fluent uses the Butler-Volmer equation. From Eqns. A12–A15, the molar concentration of the reactant species at anode and cathode electrodes are represented by \([A]\) and \([C]\) respectively. The \( A \) represents the hydrogen concentration and the \( C \) is the concentration of oxygen. The local surface overpotential driving force for the kinetics is denoted by \( \eta \). The overpotential is also referred to as the activation loss. The difference between the membrane potential and the solid potential is the overpotential. The gain in electrical potential from moving from the anode electrode to the cathode electrode is calculated by subtracting the open-circuit voltage \( V_{OC} \) of the cathode electrode.

\[
\eta_{\text{an}} = \phi_{\text{sol}} - \phi_{\text{mem}} \quad \text{[A16]}
\]

\[
\eta_{\text{cat}} = \phi_{\text{sol}} - \phi_{\text{mem}} - V_{OC} \quad \text{[A17]}
\]
Using volumetric species mass terms is also a method of adhering to mass conservation.

\[ S_{H_2} = - \frac{M_{W,H_2}}{2F} R_{an} < 0 \quad [A18] \]

\[ S_{O_2} = - \frac{M_{W,O_2}}{2F} R_{cat} < 0 \quad [A19] \]

\[ S_{H_2O} = - \frac{M_{W,H_2O}}{2F} R_{an} > 0 \quad [A20] \]

The species source term (Kg/s.m³) in this case is represented by \( S_X \) and \( M_W \) is the species molecular mass (kg/kmole). The equation has a negative sign indicating that the hydrogen and oxygen are depleting by reaction while water is formed. Conservation of electric current is described by Eq. A21 shown below.

\[ \int R_{an}dV_{an} = \int R_{cat}dV_{cat} \quad [A21] \]

The volumetric sources for thermal energy are needed because not all of the chemical energy is converted to electrical work. The thermal energy equation is used to describe the process:

\[ S_h = h_{react} - R_{an,cat} \eta_{an,cat} + I^2 R_{ohm} + h_L \quad [A22] \]

where the net rate of change in enthalpy (J/s) as a result of electrochemical reactions is represented by \( h_{react} \cdot R_{an,cat} \eta_{an,cat} \) is the product of anode overpotential and transfer current or cathode
potential and transfer current. $R_{ohm}$ is the conducting media ohmic resistivity and $I$ is the current (A). $h_L$ is the enthalpy change due phase change of water. The flow through the porous media of the gas diffusion layers and catalyst layer was also modelled by adding a negative source that represents the flow pressure drop into the species equations and computing species diffusivities. Many mathematical expressions were used to represent each process occurring at each region in the fuel cell as explained earlier. The continuity, momentum transport, energy, hydrogen transport at the anode region, oxygen transport, water transport at both the anode and cathode region can all be represented by mathematical expressions. The earlier equations (A3-A22) can also be grouped into specific sections as indicated in Table A2.
Table A2: Governing equations of the fuel cell model.

<table>
<thead>
<tr>
<th>Governing Equations</th>
<th>Mathematical expressions</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Continuity</strong></td>
<td>( \frac{\partial(p \to u)}{\partial x} + \frac{\partial(p \to v)}{\partial y} + \frac{\partial(p \to w)}{\partial z} = S_M )</td>
</tr>
</tbody>
</table>
| **Momentum transport** | a \[ \begin{align*}
    &\frac{\partial(p \to u)}{\partial x} + v \frac{\partial(p \to v)}{\partial y} + w \frac{\partial(p \to w)}{\partial z} = \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \mu \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left( \mu \frac{\partial u}{\partial y} \right) + \frac{\partial}{\partial z} \left( \mu \frac{\partial u}{\partial z} \right) + S_{px} \\
    &\frac{\partial(p \to v)}{\partial x} + \frac{\partial(p \to v)}{\partial y} + w \frac{\partial(p \to w)}{\partial z} = \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \mu \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial y} \left( \mu \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial z} \left( \mu \frac{\partial v}{\partial z} \right) + S_{py} \\
    &\frac{\partial(p \to w)}{\partial x} + v \frac{\partial(p \to v)}{\partial y} + w \frac{\partial(p \to w)}{\partial z} = \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \mu \frac{\partial w}{\partial x} \right) + \frac{\partial}{\partial y} \left( \mu \frac{\partial w}{\partial y} \right) + \frac{\partial}{\partial z} \left( \mu \frac{\partial w}{\partial z} \right) + S_{pz} \end{align*} \] |
| **Energy**           | \( \frac{\partial(pCT)}{\partial x} + v \frac{\partial(pCT)}{\partial y} + w \frac{\partial(pCT)}{\partial z} = \frac{\partial}{\partial x} \left( k \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left( k \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z} \left( k \frac{\partial T}{\partial z} \right) + S_h \) |
| **Hydrogen transport** | d \[ \begin{align*}
    &\frac{\partial(pyH_2)}{\partial x} + v \frac{\partial(pyH_2)}{\partial y} + w \frac{\partial(pyH_2)}{\partial y} = \frac{\partial(J_{x,H_2})}{\partial x} + \frac{\partial(J_{y,H_2})}{\partial y} + \frac{\partial(J_{z,H_2})}{\partial z} + S_{H_2} \\
    \end{align*} \] |
| **Water transport**  | e \[ \begin{align*}
    &\frac{\partial(pyaw)}{\partial x} + v \frac{\partial(pyaw)}{\partial y} + w \frac{\partial(pyaw)}{\partial y} = \frac{\partial(J_{x,aw})}{\partial x} + \frac{\partial(J_{y,aw})}{\partial y} + \frac{\partial(J_{z,aw})}{\partial z} + S_{aw} \end{align*} \] |
| **Oxygen transport** (Cathode) | \[ \frac{\partial (pY_{O_2})}{\partial x} + \frac{\partial (pY_{O_2})}{\partial y} + \frac{\partial (pY_{O_2})}{\partial z} = \frac{\partial (\overrightarrow{J_{x,o_2}})}{\partial x} + \frac{\partial (\overrightarrow{J_{y,o_2}})}{\partial y} + \frac{\partial (\overrightarrow{J_{z,o_2}})}{\partial z} + S_{O_2} \] |
| **Water transport** (Cathode) | \[ \frac{\partial (pycw)}{\partial x} + \frac{\partial (pycw)}{\partial y} + \frac{\partial (pycw)}{\partial z} = \frac{\partial (\overrightarrow{J_{x,cw}})}{\partial x} + \frac{\partial (\overrightarrow{J_{y,cw}})}{\partial y} + \frac{\partial (\overrightarrow{J_{z,cw}})}{\partial z} + S_{cw} \] |
| **Source terms** | \[ S_m = S_{H_2} + S_{aw} \quad S_m = S_{O_2} + S_{cw} \]
| | \[ S_{px} = \frac{\mu}{k} \quad S_{py} = \frac{\mu}{k} \quad S_{pz} = \frac{\mu}{k} \]
| | \[ \frac{\rightarrow j_i}{= \; -pD_l \nabla y_i} \]
| | \[ S_h = I^2 R_{ohm} + h_{react} + \eta_{act} R_{an,ca} \]
| | \[ S_{H_2} = -\frac{M_{H_2}}{2F} R_{an} \]
| | \[ S_{aw} = -\frac{M_{H_2O}}{F} R_{an} \]
| | \[ S_{aw} = -\frac{M_{O_2}}{4F} R_{ca} \]
| | \[ S_{cw} = -\frac{M_{H_2O}}{2F} R_{ca} \] |
| Charge Transport | $\nabla \cdot (\sigma_{\text{Sol}} \nabla \phi_{\text{Sol}}) + R_{\text{Sol}} = 0$ | $\nabla \cdot (\sigma_{\text{mem}} \nabla \phi_{\text{mem}}) + R_{\text{mem}} = 0$ | P |
Boundary conditions

The cell temperature for this study was kept at 80°C for both the experimental work and the simulation. The detailed boundary conditions and zones used in the simulation work are shown in Tables A3 – A5. The different simulation runs conducted for the separate designs required different times for convergence to occur. From literature [35] more time is required for convergence to occur at higher flow rates than at lower flow rates due to the fact that the low flow rate involves the Stefan-Maxwell equation (Full multicomponent diffusion method) which is used in the simulation instead of the Fick’s law (Dilute approximation method) that is used for high flow rates thus making the computational model more complex with the values set for under-relaxation factors in Fluent being reduced to enable the calculations to reach stability.

In order to confirm convergence of simulations in this study, an approach similar to that used by Arvay et al [36] is used. In their work, they reported that using the residual monitoring alone was not enough to confirm convergence of the simulations and another indicator such as confirming the consistency of the calculated voltage and comparing the current calculated from the amount of the consumed fuel mass with the boundary current is required.

Table A3: Boundary zone assignment

<table>
<thead>
<tr>
<th>Anode inlet</th>
<th>Inlet – anode</th>
<th>Mass flow inlet</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cathode inlet</td>
<td>Inlet – cathode</td>
<td>Mass flow inlet</td>
</tr>
<tr>
<td>Anode outlet</td>
<td>Outlet – anode</td>
<td>Pressure outlet</td>
</tr>
<tr>
<td>Cathode outlet</td>
<td>Outlet – cathode</td>
<td>Pressure outlet</td>
</tr>
<tr>
<td>Anode terminal</td>
<td>Terminal – anode</td>
<td>Wall</td>
</tr>
<tr>
<td>Cathode terminal</td>
<td>Terminal – cathode</td>
<td>Wall</td>
</tr>
<tr>
<td>Anode flow field</td>
<td>Ch – a</td>
<td>Wall</td>
</tr>
<tr>
<td>Cathode flow field</td>
<td>Ch – c</td>
<td>Wall</td>
</tr>
<tr>
<td>Anode current collectors</td>
<td>Cc - a</td>
<td>Wall</td>
</tr>
<tr>
<td>Cathode current collectors</td>
<td>Cc - c</td>
<td>Wall</td>
</tr>
<tr>
<td>Anode gas diffusion layer</td>
<td>Diff-a</td>
<td>Wall</td>
</tr>
<tr>
<td>Cathode gas diffusion layer</td>
<td>Diff-a</td>
<td>Wall</td>
</tr>
</tbody>
</table>
Table A4: Boundary conditions

<table>
<thead>
<tr>
<th>Boundary conditions</th>
<th>Type</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anode Inlet</td>
<td>Mass flow inlet</td>
<td>6.0 x 10^{-7}</td>
<td>Kg/s</td>
</tr>
<tr>
<td>Cathode Inlet</td>
<td>Mass flow inlet</td>
<td>5.0 x 10^{-6}</td>
<td>Kg/s</td>
</tr>
<tr>
<td>Anode – outlet</td>
<td>Outlet Pressure</td>
<td>200000 (2bar)</td>
<td>Pascals</td>
</tr>
<tr>
<td>Cathode – Outlet</td>
<td>Outlet Pressure</td>
<td>200000 (2bar)</td>
<td>Pascals</td>
</tr>
<tr>
<td>Anode – Wall</td>
<td>Wall</td>
<td>No slip</td>
<td>-</td>
</tr>
<tr>
<td>Cathode – Wall</td>
<td>wall</td>
<td>No slip</td>
<td>-</td>
</tr>
</tbody>
</table>

Table A5: Zone assignments

<table>
<thead>
<tr>
<th>Zone assignment</th>
<th>Zone Type</th>
<th>Fluidity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anode catalyst layer</td>
<td>Catalyst – anode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Cathode catalyst layer</td>
<td>Catalyst – cathode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Anode flow field</td>
<td>Ch – anode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Cathode flow field</td>
<td>Ch – cathode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Anode gas diffusion layer</td>
<td>Diff – anode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Cathode gas diffusion layer</td>
<td>Diff – cathode</td>
<td>Fluid</td>
</tr>
<tr>
<td>Membrane</td>
<td>Mem</td>
<td>Fluid</td>
</tr>
<tr>
<td>Anode collector</td>
<td>cc- anode</td>
<td>Solid</td>
</tr>
<tr>
<td>Cathode collector</td>
<td>cc- cathode</td>
<td>Solid</td>
</tr>
</tbody>
</table>

To prevent divergence in the calculations and water saturation, the source term value and the water saturation under relaxation factor were kept low and this made the convergence of the water saturation value very slow. It was observed that after more than 1500 iterations, the voltage and current usually converged but the water saturation value took longer time before converging when the source term and water saturation under relaxation factors were kept between 0.7 and 0.05.

Another approach suggested by Iranzo et al [38] was also considered for monitoring convergence. This is based on monitoring the average value of the membrane water content and water saturation.
The solution procedure utilized the Semi-Implicit Method for Pressure Linked Equations (SIMPLE) algorithm. This algorithm is a guess and correct method in which the pressure and velocities were calculated and updated in all the iterations.

For a well refined computational grid, the speed with which the solution will converge becomes fast and the algebraic multigrid (AMG) was also used to help with the convergence process. The second order upwind solver discretization scheme was used in the simulations.

The open circuit voltage was set at 1.2V. The anodic and cathodic electrode zones were clearly defined in the mesh and named as shown in Table A5 above. The active area of the fuel cell was 25mm². With the exception of the current collectors for each electrode of the fuel cell, all other parts were defined as fluid zones. The mathematical description of the mass flow rate is shown in Eq. A23.

\[ \eta_{\text{reactant}} = \frac{iA}{nF} \]  

where \( i \) is the current density, \( A \) is the active area of the PEMFC which is 25mm² (0.0025m²), \( n \) represents the various oxidation numbers for hydrogen and oxygen which are 2 and 4, respectively, and \( F \) is the Faraday’s constant which is 96,485 C mol⁻¹.

The mass fractions of the species at the inlet of the anode were set to 0.8 for hydrogen and 0.2 for water. The mass fractions of the species at the cathode inlet were set at 0.2 for oxygen and 0.1 for water. The operating pressure and temperature for the entire simulation for all the humidification conditions were maintained at 2 bar and 353 K, respectively.
Appendix B: Experimental Validation of Simulation Results

The experimental results from this study as well as other earlier reported results from Cheng et al. [40] were used to validate the results obtained from the simulation model developed in this study.

The parameters used in the laboratory experiment were the same as those used in the CFD simulations.

The fuel cell used in the experiments is a one cell stack PEM fuel cell made of Nafion membrane. The surface area of the fuel cell (active area) was 25cm$^2$ with a thickness of 27µm and a platinum catalyst layer loading of 0.3 mg Pt/cm$^2$. Pure hydrogen is used as fuel supply and this was provided by a hydrogen generator. A flow meter was used to determine the flow rate of the gas and the supply of the hydrogen to the fuel cell was in dead end mode as shown in Fig B1. It implies that all the hydrogen supplied was assumed to be consumed by the fuel cell.

Fig. B1. Dead end mode (Rate of hydrogen supplied is equal to rate of hydrogen consumed)

To keep the hydrogen gas constantly pressurized, a valve was attached to the anode region of the fuel cell and this valve was often opened to allow the by-product of the electrochemical reaction to leave the fuel cell. The fuel cell used was air breathing and it is shown in Fig. B2.
Fig. B2: Air channels for oxygen supply.

A fan was attached to the cell to help in cooling and also functioned as oxygen (air) supply to the fuel cell. The experimental set up is shown schematically in Fig. B3 and Fig. B4.

Fig. B3: Schematic drawing of the fuel cell testing set up

Fig. B4: Experimental set up showing the various connections and hydrogen generator.

The setup consists of a hydrogen generator for supplying pure hydrogen to the fuel cell through an electrolytic process. The pressure of the hydrogen leaving the hydrogen generator was controlled and kept constant. The hydrogen gas was then channelled through a flow meter that measured the
gas flow rate. The hydrogen was then humidified by passing it through a humidification chamber as shown in Fig. B5.

A Gamry potentiostat was used to determine the characteristic performance of the fuel cell and a thermocouple was attached to the fuel cell to measure its operating temperature. The humidification chamber was filled with water and the temperature of the water was manipulated using a hot plate as shown in Fig. B5.