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On the achievable rate of hybrid precoding for hardware impaired MIMO underground mine channel

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Hybrid precoding has become a well-accepted approach to enhance the achievable rate in the adverse underground mm-Wave communications. To overcome this limitation, in this letter, a new architecture encompassing hybrid precoded mm-Wave MIMO structure is proposed. In this architecture, the hardware impairments have been incorporated in the transceiver processing, is presented. Furthermore, the geometrical one ring model is applied on the underground mm-Wave measured channel on which the architecture is tested.

Introduction: Because of the future applications targeting underground mining environments, such as the wireless video, which are greedy in terms of data rate resources, different solutions offering such resources are sought. Owing to their large available bandwidth, millimeter-Wave (mm-Wave) communications are presenting themselves as a quite viable technology to fulfill such requirements, and the measurement campaigns to characterize such channels at this frequency band and adapt the communication to them, have already been launched [1]. One of the biggest impediments to mm-Wave underground propagation is the presence of materials with different dielectric and conductive properties, of irregularities along the walls, as well as the high path loss, which hinder the communication scheme throughout enhancement [2]. To bridge the resulting significant link budget gap in such environments, directional multiple antennas have been recently adopted. Interestingly, scaling up the number of antennas, hence achieving a large spatial degree of freedom (DoF), yields a higher spectral efficiency (SE) and mitigates the effects of the channel fading [3, 4, 5, 6]. However, most prior works on MIMO wireless systems neglect realistic aspects pertaining to the real deployment of the communication system, such as the imperfections of the transceiver hardware. Indeed, it is agreed upon that hardware components in a practical system experience various impairments, including the oscillator phase noise (PN) and the 60 GHz power amplifier (PA) undesirable effects [7]. Motivated by this, this work proposes a hybrid precoding architecture, in which the previously mentioned hardware imperfections were included and compensated. The proposed solution is tested over the mm-Wave measured underground mine channel. Another contribution of this letter lies in the extension of the newly proposed 2-D geometrical scattering one ring-based model on measurements carried out in a mine in Northern Canada at the 60 GHz band. To the best of our knowledge, neither the design of such a hardware impairments-aware scheme combining hybrid precoding-aided mm-Wave communications has been proposed before, nor the representation of underground channel with a 2-D geometrical scattering model has been targeted previously. The proposed architecture aims at enhancing the achievable rate performance in the adverse underground wireless mm-Wave channels, while reducing the impairment of hardware transceivers practical defects on it. Our results corroborate that the architecture indeed meets such objectives in a viable way.

System model: Let us consider a hybrid precoding architecture deployed in a mm-Wave underground channel, wherein the transmitter and the receiver are equipped with $N_t$ and $N_r$ elements, respectively, as illustrated in Fig. 1. We assume that $N_{RF}$ radio frequency (RF) chains are employed at the transceiver such that $N_{RF} \leq N_t$, $N_{RF} \leq N_r$, and that the total number of streams is $N_s = N_{RF}$. In order to implement this architecture, the transmitter applies two consecutive precoding operations, $F_{bb} \in C^{N_s \times N_{RF}}$, and $F_{RF} \in C^{N_{RF} \times N_{RF}}$, where the former refers to the digital baseband precoder, whilst the latter denotes the analog counterpart. The received signal can be then represented as

$$y = HF_{RF}F_{bb}x + n,$$ (1)

where $x \in C^{N_s \times 1}$ is the transmitted symbol, of which the covariance matrix is $Q = E[x|x] = \frac{1}{P_t}I_{N_s}$, with $P_t$ being the total transmit power, $F_{bb} = F_{bb}F_{bb}^H$ is the hybrid precoder, $h \in C^{N_r \times N_s}$ is the underground mine channel at the mm-Wave band emulated using the 2-D geometrical model, and $n \sim C(0, \sigma^2)$ represents the additive white Gaussian noise (AWGN) at the receiver, where $\sigma^2$ stands for the noise variance.

At the receiver side, the combiner $W_{bb}W_{RF}$, which is composed of an RF combiner $W_{bb} \in C^{N_r \times N_{RF}}$ and a digital one $W_{RF} \in C^{N_{RF} \times N_{RF}}$, is used to extract the transmitted data from the received signal, which could be expressed as follows:

$$y = W_{RF}H_{RF}F_{bb}x + W_{RF}n.$$ (2)

This model implicitly assumes ideal transceiver hardware. To consider the impact of transceiver impairments which has been discussed in massive MIMO systems in [7], equation (2) can be modified as follows:

$$y = W_{RF}^{(2)}H_{RF}(F_{bb} + \eta_I) + W_{RF}^{(2)}n.$$ (3)

where $W = W_{RF}^{(2)}n$ and $\eta_I$ refer to the transceiver impairments residue in the transmitter and the receiver hardwares, respectively, which are assumed to be independent of the transmitted signal. These terms are modelled as

$$\eta_I \sim C(0, k_s^2 \text{diag}(\{q_1^2, \ldots, q_L^2\})), \quad \eta_J \sim C(0, b^2 \text{tr}(Q)I_{N_s}),$$ (4)

where the coefficients $k_s$ and $k_J$ are characterizing the levels of impairments at the transmitter and the receiver, respectively, with $q_l$ denoting the $l^\text{th}$ diagonal element of the signal covariance matrix $Q$, and $\text{tr}()$ stands for the trace of the matrix.

**Fig. 1.** Transceiver structure of hybrid mm-Wave MIMO system.

Geometrical-based Underground mine channel model: The geometrical one ring model for MIMO underground mine channel is shown in Fig. 2, in which the transmitter is equipped with $N_t$ antennas and the receiver with $N_r$ antennas. It assumes that there are $k$ scatterers $S_l (l = 1, \ldots, L)$ located on a ring, with a radius $R$ around the receiver. The measurements carried out in a real underground mine operated by the Canadian Center for Minerals and Energy Technology (CANSMET) are exploited in our model. During the experiments, the transmitter (Tx) is maintained fixed, while the receiver (Rx) was moved at different positions along the gallery, from 1 m up to 10 m, with steps of 1 m in [1].

**Fig. 2.** Geometrical one ring model for a MIMO Underground mine channel [8].

In the one-ring model the path length from the $t^\text{th}$ transmit antenna to the $r^\text{th}$ receive antenna via the $l^\text{th}$ scatterer is obtained through geometrical considerations as a function of $D$:
where $\alpha = \arcsin \left( \frac{r}{D} \right)$ is the angle of arrival of the $l$th scatterer, and $D$ is the distance between the Tx and Rx. Thus, the corresponding channel in the $v$th - $v'$th link is given by:

$$H_{v,v'} = \frac{1}{\sqrt{L}} \sum_{l=1}^{L} \sqrt{\frac{\gamma_{i,l}}{\gamma_{r,l}}} \left( -j \left( 2 \pi \sigma_{l} d_{l}^{2} + R \right) \right)$$

where $\gamma_{i,l}$ is the $l$th measured time domain path loss obtained from the channel impulse response, for any fixed location between Tx and Rx, $d_{l}$ is the phase shift associated with each scatter $S(\alpha)$, which is assumed in our case as uniformly distributed in the interval $[-\pi, \pi].$

**Simulation Results:** In this section, the achievable rate performance is investigated for the proposed system incorporating hybrid precoding technique, over the MIMO underground mine channel, for which measurements have been fitted using geometrical model. Analog beamforming, implemented within a similar architecture as the proposed scheme, and relying on the one-ring channel model, is taken as a reference to study the performance penalty with hardware defaults. The system considers the practical hardware imperfections at the both transmitter and receiver sides, and is operating in the frequencies ranging from 57 to 62 GHz, thus has a bandwidth of 500 MHz. Furthermore, it is assumed that the transmitter and the receiver are equipped with equal number of antenna elements, the number of RF chains $N_{RF} = 2$ and the number of scatterers in the geometrical model has been assumed as $L = 3$. Based on this, the normalized achievable rate $R$ of hybrid precoding scheme incorporating transceiver hardware impairments could be formulated as:

$$R = \log_{2}(\det[I_{k_{t}} + \frac{1}{\gamma} \Phi^{H}\Phi])$$

where $\Phi = \gamma_{i}[F^{H}F] + \gamma_{i}^{2}I + \lambda I$, $I_{k_{t}}$ represents the hardware impairments, and $\gamma$ is the signal to noise ratio (SNR).

The simulation investigates the result of increasing the effect of hardware impairments on the proposed system. For this purpose, the parameters $k_{t}$ and $k_{r}$ are varied to emulate the variation of the degree of impairments from high to non-existent, and, without loss of generality, the numbers of transmit and receive antennas are both equal to 10. From Fig. 3 comparing the behaviour of the proposed scheme along with analog beamforming alternative face to hardware defaults, it is seen that a performance loss is noted relative to the idealistic hardware operation conditions, more particularly with analog beamforming, and increases substantially as the impairment level gets higher. The presence of these practical imperfections induces a saturation phenomena in the achieved rate at relatively high SNR values, where the increase of the transmit power brings no gain in the performance. It is also observed that analog beamforming-based system experiences a critical performance penalty which exceeds 6 dB, when the hardware conditions vary from being ideal to undergoing an impairment factor of 0.25 at both the transmitter and the receiver sides. By contrast, the proposed solution exhibits a significant robustness to such hardware deviations from ideal case, and the corresponding noted performance losses remain quite reasonable. The presented architecture outperforms analog beamforming-based alternative regardless of the conditions of operations of the hardware, and is then more appropriate for practical deployments in such underground channels.

**Conclusion:** This letter considers the hardware distortions, pertaining to the transmit and receiver RF chains, in the design of the hybrid precoded mm-Wave MIMO architecture, deployed in underground channels. We have applied a 2-D geometrical channel model, which is based on one ring configuration, to describe the propagation mechanism in our underground channel, and achievable rate performance was investigated based on this model and the modified transceiver structure. The higher performance and robustness against hardware imperfections of the proposed solution, relative to analog beamforming-based counterpart, have been demonstrated in these MIMO underground environments.

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